Analysis of a national low dc resistance inter-laboratories comparison

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Abstract. In this paper the description of an inter-laboratories comparison between the National Institute of Metrological Research (INRIM) and nineteen Italian Secondary Calibration Electrical Laboratories, is given along with its main results in graphical way. The transportable standards were three Tinsley four terminal standard resistors to be calibrated in oil respectively at 5 A and 20 A (1 mΩ), 1 A and 5 A (10 mΩ), 0.1 A and 1 A (100 mΩ). The comparison results were satisfactory, except only in a case of a Laboratory for which these measurements were outside its accreditation fields.

1 Introduction

An inter-laboratory comparison aims to verify the compatibility of the measures of two or more Laboratories performed on the same measurand within their measurement uncertainties. Since its start the Italian Calibration Laboratories body (formerly “Servizio di Taratura in Italia” SIT) used to perform bilateral comparisons between the National Metrology Institutes and the Secondary calibration Laboratories to evaluate their technical competence in the framework of their first accreditation or in the periodical renewal of their accreditation. Normally, the results were elaborated according to the ISO Guide 43. Nowadays the number of Secondary Laboratories grew significantly, so the possibility to perform bilateral comparisons became quite difficult. A possible solution for this problem could be the use accredited of Inter-laboratory Comparisons providers (ILCs) [1, 2]. In this occasion the Italian Accreditation body (now ACCREDIA) gave to the National Institute of Metrological Research (INRIM) the task to perform an inter-laboratories comparison between INRIM and nineteen Italian Secondary calibration Electrical accredited Laboratories in the field of low dc resistance. The transportable standards for the comparison were three Tinsley mod 3504C 1 mΩ, 10 mΩ and 100 mΩ four terminal standard resistors to be calibrated respectively at 5 A and 20 A (1 mΩ), 1 A and 5 A (10 mΩ), 0.1 A and 1 A (100 mΩ). View of the model of these standards is given in Figure 1 and 2. The participating Laboratories were:

- ASIT INSTRUMENTS, Orbassano (TO), accredited calibration laboratory (acl) 188;
- ARO, Biassono (MI) acl 46;
- AVIATRONIK, Samarate -(VA) acl 19;
- CERMET, Bologna, acl 52;
- DELO Services. s.r.l., Fizzonasco Pieve (MI), acl 121;
- EMIT LAS, Milan, acl 24;
- FASINTERNATIONAL, Milan, acl 128;
- GAMMA MISURE, Calenzano - (FI), acl 56;
- IMQ, Milan acl 21.
- METRA, Augusta (SR), acl 188.
- METRIX, S. Stefano Cisquina (AG), acl 171.
- NEMKO, 4 Biassono (MI) acl 42;
- QUALITY SERVICE, Venice, acl 112;
- SIMAV S. Maurizio Can. - TO) acl 64.
- SIMAV, Milan, acl 04;
- TECHNO SKY, Rome .acl 15;
- TELECOM, Turin, acl 72;
- TESI, Subbiano (AR), acl 101;

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3 Travelling Standards

The transportable standards for the comparison were three Tinsley mod 3504C 1 mΩ, 10 mΩ and 100 mΩ four terminal standard resistors to be calibrated respectively at 5 A and 20 A (1 mΩ), 1 A and 5 A (10 mΩ), 0.1 A and 1 A (100 mΩ). View of the model of these standards is given in Figure 1 and 2. The travelling package included

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also a thermal collector for each resistor (Figure 1) to be inserted in the resistors to be in thermal contact with them and suitable to measure their temperature and a glass beaker to be filled with 500 ml of mineral oil. The measurements had to be carried out placing resistors inside it and acquiring the regime temperature of the thermal collector inside the resistor (Figure 2).

Before the start of the comparison the three resistors were characterized evaluating their power and temperature coefficients. These measurements were made by the Low Resistances Calibration Laboratory of INRIM and performed with a measurement method involving high precision standard resistors put in a thermo-regulated at 23±0.3 °C oil-bath, a high performance current comparator bridge and a high stability power supply [3, 4]. The travelling resistors were placed in another thermo-regulated oil-bath with similar characteristics. The evaluated temperature and power coefficients of the travelling resistor are reported in Table 1 and 2.

### Table 1. Temperature coefficients of the travelling resistors.

<table>
<thead>
<tr>
<th>Resistor</th>
<th>α</th>
<th>β</th>
</tr>
</thead>
<tbody>
<tr>
<td>1 mΩ</td>
<td>≈1.0×10⁻⁷°C</td>
<td>≈-6.0×10⁻⁷°C²</td>
</tr>
<tr>
<td>10 mΩ</td>
<td>≈9.3×10⁻⁸°C</td>
<td>≈5.5×10⁻⁷°C²</td>
</tr>
<tr>
<td>100 mΩ</td>
<td>≈-8.9×10⁻⁶°C</td>
<td>≈-4.7×10⁻⁷°C²</td>
</tr>
</tbody>
</table>

### Table 2. Power coefficients of the travelling resistors.

<table>
<thead>
<tr>
<th>Resistor</th>
<th>Power coeff</th>
</tr>
</thead>
<tbody>
<tr>
<td>1 mΩ</td>
<td>≈4.1×10⁻⁸/mW</td>
</tr>
<tr>
<td>10 mΩ</td>
<td>≈3.7×10⁻⁹/mW</td>
</tr>
<tr>
<td>100 mΩ</td>
<td>≈-8.1×10⁻⁹/mW</td>
</tr>
</tbody>
</table>

### 3.1 Time drift of the travelling resistors

The 1 mΩ resistor showed a high stability following a 2nd order polynomial drift of about 1.6×10⁻⁸/day and 3.0×10⁻⁹/day, respectively at 5 A and 20 A during the whole period in the INRIM measurements, with only a small rise in the middle period.

Also the 10 mΩ resistor showed a high stability with a 2nd order polynomial drift of about 3.8×10⁻⁹/day and 2.9×10⁻⁹/day, respectively at 1 A and 5 A during the whole period of the comparison in the INRIM measurements, with also in this case a small rise in the middle period at 1 A, and smoothly decreasing at 5 A.

![Figure 1](image1.png)

**Figure 1.** Tinsley mod 3504C resistor with the thermal collector to put inside.

![Figure 2](image2.png)

**Figure 2.** Tinsley mod 3504C resistor with the thermal collector inside the glass beaker.

![Figure 3](image3.png)

**Figure 3.** INRIM measurements 2nd order polynomial fit of the 1 mΩ resistor at 5 A.

![Figure 4](image4.png)

**Figure 4.** INRIM measurements 2nd order polynomial fit of the 10 mΩ resistor at 1 A.
Finally also the 100 mΩ resistor showed a high stability with linear decreasing drift of about $4.4 \times 10^{-9}$/day both at 0.1 A and 1 A during the whole period of the comparison in the INRIM measurements.

![Figure 5](image-url) INRIM measurements linear fit on the 100 mΩ resistor at 0.1 A.

### 3.2 Calibration modalities

The Laboratories had to perform the calibration of the resistors in four-terminal configuration at the current values and time applications shown in Table 3. If the adopted measurement method did not allow the choice of the measuring current, the applied current value and its application time had to be stated. Before starting the measurements it was suggested to wait two hours to stabilize the resistors in the oil. After performing the measurement at higher current, if was suggested to repeat the cycle after a waiting time of four hours. The reference ambient temperature of the laboratory had to be 23 °C and the Laboratory had to indicate the ambient temperature at the time of calibration. The Laboratory had to acquire also the temperature at the thermal regime reached for each measurement current. This temperature had to be measured at the thermal shaft junction of the resistor with a thermometer or a temperature sensor; these values allowed to correct at 23 °C the Laboratories measurements for a more correct evaluation of the compatibility with respect INRIM.

<table>
<thead>
<tr>
<th>Resistor</th>
<th>Meas. currents</th>
<th>Application times</th>
</tr>
</thead>
<tbody>
<tr>
<td>1 mΩ</td>
<td>5 A</td>
<td>5 min</td>
</tr>
<tr>
<td></td>
<td>20 A</td>
<td>15 min</td>
</tr>
<tr>
<td>10 mΩ</td>
<td>1 A</td>
<td>5 min</td>
</tr>
<tr>
<td></td>
<td>5 A</td>
<td>15 min</td>
</tr>
<tr>
<td>100 mΩ</td>
<td>0.1 A</td>
<td>5 min</td>
</tr>
<tr>
<td></td>
<td>1 A</td>
<td>15 min</td>
</tr>
</tbody>
</table>

**Table 3:** Resistors under calibration along with currents and their application times.

### 4 Measurement procedures

The INRIM measurements were carried out with the previously mentioned measurement system involving high precision standard resistors and an high performance current comparator. The participating Secondary Laboratories measured the three standard resistors following their measurement procedures. In particular the involved measurement methods were:

- Direct reading with a digital multimeter (DMM), in particular for the 100 mΩ standard at 0.1 A. For the other measurement points this method didn’t allow to perform the measurements at upper current values, so those measurements were considered as not accredited ones.
- Substitution method with a standard shunt or resistor connected in series with the resistor under calibration and supplied by a high stability current source (multifunction calibrator) and a DMM to measure the voltage drops on the standard and under calibration resistors.
- Volt-ampere-metric method with a high precision current source (multifunction calibrator) and a DMM to measure the voltage drop on the resistor under calibration.

### 5 Analysis of the results

To evaluate the measurement comparison the results of each measurement point were analyzed in the same way of [5, 6]. The measurement values obtained by the Laboratories and by INRIM were defined respectively as: $m_{\text{Lab}} \pm u_{\text{Lab}}$ and $m_I \pm u_I$ (1)

where $m_{\text{Lab}}, u_{\text{Lab}}, m_I, u_I$ are respectively the measurement values and the standard uncertainties of the Laboratories and of INRIM. Both INRIM and the Laboratories gave their results along with the reached regime temperature at each measurement current, so that all the measurement values were reported at the temperature of 23.0 °C, starting from their temperature coefficients. For $m_I$ were taken into account the interpolated values of INRIM measurements at the date of the measurements of the Laboratories. With this interpolation, an uncertainty due to possible errors due to the fitting operation was added to the INRIM uncertainty. A new measurand:

$$y_{\text{Lab}} = (m_{\text{Lab}} - m_J)/m_I$$

was defined for each measurement point whose relative standard uncertainty is:

$$u_{y_{\text{Lab}}}^2 = \frac{1}{m_I^2} \times \left[ u_{\text{Lab}}^2 + u_J^2 - 2u_{\text{Lab}} u_J \times r(m_{\text{Lab}}, m_J) \right]$$

where $r(m_{\text{Lab}}, m_J)$ is the correlation factor between the measurements of the Laboratories and those of INRIM, evaluated as the ratio between the type B component of the uncertainty with which INRIM calibrated the...
reference standards of the Laboratories and the uncertainty declared by the same Laboratories for the comparison. Finally, the normalized error $En$ with respect to INRIM for each measurement point and for each Laboratory was evaluated as:

$$En = \frac{y_{\text{Lab},r}}{U_{\text{Lab},r}}$$

$$U_{\text{Lab},r} = 2u_{\text{Lab},r} 2\sigma$$

(4)

6 Measurement results

In Figure 6, the normalized errors $En$ for each participant Laboratory and for each resistor and measurement current are reported as an estimate of the compatibility degree with INRIM measurements. In Figures from 7 to 12 INRIM and Laboratories results corrected at 23 °C with their $2\sigma$ uncertainties, are shown.

Figure 6. Laboratories normalized errors.

In Figures from 7 to 12 INRIM and Laboratories results corrected at 23 °C with their $2\sigma$ uncertainties, are shown.

Figure 7. Results for the 1 mΩ at 5 A.

Figure 8. Results for the 1 mΩ at 20 A.

Figure 9. Results for the 10 mΩ at 1 A.

Figure 10. Results for the 10 mΩ at 5 A. Lab 5 did not make this measurement.
7 Discussion

The condition that has to be satisfied for a correct traceability transfer from National Standards is that $E_n < |1|$. In figure 6 it is shown that the majority of the measurement points satisfied this condition. It was accurately verified that all the measurements performed under accreditation satisfied the previous condition. In fact the measurements with $E_n > |1|$ were made in particular by a Laboratory that, although accredited for dc resistance, these fields are out of its accreditation field. Other border line $E_n$ values were from Laboratories that were not able to perform the measurements at the correct currents (for example reading directly with a DMM) but issued calibration certificates according to their accredited procedures. Considering all these conditions it can be concluded that the traceability transfer to Secondary Electrical Laboratories the field of low dc resistance is correctly assured.

References